

SET FOR DEPT'T.  
2.1, 2.2 (m) Paper.

3 (Sem-2) PHY M 1

2018

PHYSICS

( Major )

Paper : 2.1

Full Marks : 60

Time : 3 hours

The figures in the margin indicate full marks  
for the questions

GROUP—A

( Mathematical Methods-II )

( Marks : 35 )

1. Answer the following questions : 1×3=3

(a) Evaluate  $\vec{a} \times \frac{d^2 \vec{r}}{dt^2} = \vec{b}$ , where  $\vec{a}$  and  $\vec{b}$  are constants.

(b) Define Laplacian in curvilinear coordinate system.

(c) Evaluate  $\Gamma(-\frac{1}{2})$ .

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2. Find the value of  $\iint_S \vec{r} \cdot \hat{n} dS$ , where  $S$  is closed surface. 2

3. Answer any *two* of the following questions :

5×2=10

- (a) (i) Find the value of  $\int_C \vec{F} \times d\vec{r}$ , where

$\vec{F} = xy\hat{i} - z\hat{j} + x^2\hat{k}$  and  $C$  is the curve  $x = t^2$ ,  $y = 2t$ ,  $z = t^3$  from  $t = 0$  to  $t = 1$ . 3

- (ii) If  $S$  be a closed surface and  $\vec{r}$  denotes the position vector of any point  $(x, y, z)$  measured from origin  $O$ , then show that

$$\iint_S \frac{\hat{n} \cdot \vec{r}}{r^3} dS = 0$$

when  $O$  lies outside the closed surface  $S$ . 2

- (b) (i) Express the acceleration  $\vec{a}$  of a particle in cylindrical coordinates. 3

- (ii) Represent the vector  $\vec{A} = z\hat{i} - 2x\hat{j} + y\hat{k}$  in cylindrical coordinates. 2

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( Continued )

( 3 )

- (c) (i) Evaluate  $\int_0^\infty x^{n-1} e^{-h^2 x^2} dx$ . 3

- (ii) Prove that  $x\delta(x) = 0$ . 2

4. Answer any *two* of the following questions :

10×2=20

- (a) (i) Find the value of

$$\iint_S (\vec{\nabla} \times \vec{F}) \cdot \hat{n} dS$$

for  $\vec{F} = (y - z + 2)\hat{i} + (yz + 4)\hat{j} - xz\hat{k}$ , where  $S$  is the surface of the cube  $x = y = z = 0$ ,  $x = y = z = 2$  above the  $xy$ -plane. 5

- (ii) If  $R$  is a closed region in the  $xy$ -plane bounded by a simple closed curve  $C$ , and  $M$  and  $N$  are continuous functions of  $x$  and  $y$  having continuous derivatives in  $R$ , then show that

$$\oint_C (M dx + N dy) = \iint_R \left( \frac{\partial N}{\partial x} - \frac{\partial M}{\partial y} \right) dx dy$$

where  $C$  is traversed in the positive direction. 5

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( Turn Over )

( 4 )

- (b) (i) Prove that

$$\iiint_V \vec{\nabla} \phi dV = \iint_S \phi \hat{n} dS \quad 5$$

- (ii) If the normal surface integral of a vector point function  $\vec{G}$  over every open surface is equal to the tangential line integral of another function  $\vec{F}$  round its boundary, prove that  $\vec{G} = \text{curl } \vec{F}$ . 5

- (c) (i) Express  $\vec{\nabla} \times \vec{A}$  and  $\nabla^2 \psi$  in spherical coordinates. 2+3=5

- (ii) Find the element of arc length on a sphere of radius  $a$ . 5

GROUP—B

( Properties of Matter )

( Marks : 25 )

5. Answer the following questions : 1×4=4

- (a) Write the expression for Young's modulus, when increase in length is not proportional to applied force.
- (b) Draw the stress-strain graph for a wire.

( 5 )

- (c) What is the cause of surface tension of a liquid?

- (d) What will happen to angle of contact of a liquid, when the temperature increases?

6. Answer the following questions : 2×3=6

- (a) The volume of a solid does not vary with pressure. Find Poisson's ratio for the solid.
- (b) Distinguish between wave and ripple.
- (c) How does the viscosity of liquids and gases vary with temperature?

7. Answer any one of the following questions : 5

- (a) (i) Show that tensile strain in a filament is directly proportional to its distance from the neutral axis. 3
- (ii) A steel wire of length 2 m is stretched through 2 mm. The cross-sectional area of the wire is  $40 \text{ mm}^2$ . Calculate the elastic potential energy stored in the wire in the stretched condition. Young's modulus of steel  $= 2 \times 10^{11} \text{ N/m}^2$ . 2

( 6 )

- (b) (i) Write down the limitations of Poiseuille's formula for the rate of flow of liquid through a capillary tube.

3

- (ii) In the Poiseuille experiment, the following observations were made :

Volume of water collected in

5 minutes = 40 c.c.

Head of water = 0.4 m

Length of capillary tube = 0.602 m

Radius of capillary tube

$= 0.52 \times 10^{-3}$  m

Calculate the coefficient of viscosity of water.

2

8. Answer either (a) or (b) :

10

- (a) (i) Derive an expression for the twisting couple per unit angular twist for a solid cylinder.

Using the above relation, find the twisting couple per unit twist for hollow cylinder.

5+2=7

- (ii) Explain with reason, why a hollow cylinder is stronger than a solid cylinder of same length, mass and material.

3

( 7 )

- (b) (i) Show that the excess pressure acting on a curved surface of a curved membrane is given by

$$P = 2T \left( \frac{1}{r_1} + \frac{1}{r_2} \right)$$

where  $r_1$  and  $r_2$  are the radii of curvature and  $T$  is the surface tension of the membrane.

Using the above relation, calculate the excess pressure for cylindrical film.

5+2=7

- (ii) Two soap bubbles of radii  $a$  and  $b$  coalesce to form a single bubble of radius  $c$ . If the external pressure is  $P$ , show that the surface tension is given by

$$S = \frac{P(c^3 - a^3 - b^3)}{4(a^2 + b^2 - c^2)}$$

3

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